

Name: _____

Date: _____

Find the derivative.

1) $f(x) = \frac{8}{\sqrt{x}} - \frac{3}{x} + \frac{6}{x^5}$

1) _____

A) $f'(x) = -\frac{4}{x^{3/2}} - \frac{3}{x^2} - \frac{30}{x^4}$

B) $f'(x) = -4\sqrt{x} + \frac{3}{x^2} - \frac{30}{x^4}$

C) $f'(x) = -\frac{4}{x^{3/2}} + \frac{3}{x^2} - \frac{30}{x^6}$

D) $f'(x) = \frac{4}{x^{1/2}} - \frac{3}{x^2} - \frac{30}{x^6}$

Find $f'(a)$ for the given value of a .

2) $f(x) = -x^{-5} + x^{-3}$, $a = 1$

2) _____

Find the equation of the line tangent to the graph of the function at the indicated point.

3) $f(x) = \frac{27}{x}$ at $(1, 27)$

3) _____

Find all values of x (if any) where the tangent line to the graph of the function is horizontal.

4) $y = x^3 + 2x^2 - 175x + 25$

4) _____

Differentiate.

5) $g(x) = (x^{-5} + 3)(x^{-3} + 5)$ 5) _____

A) $g'(x) = -8x^{-9} - 25x^{-4} - 9x^{-4}$
B) $g'(x) = -8x^{-9} - 25x^{-6} - 9x^{-4}$
C) $g'(x) = -8x^{-9} - 25x^{-6} - 9x^{-2}$
D) $g'(x) = -8x^{-7} - 25x^{-6} - 9x^{-4}$

6) $f(x) = \sqrt[3]{x^8 + 6x}$ 6) _____

A) $f'(x) = \frac{1}{3}(x^8 + 6x)^{-2/3}$
B) $f'(x) = \frac{1}{3}(x^8 + 6x)^{-2/3}(8x^7 + 6)$
C) $f'(x) = \frac{1}{3}(x^8 + 6x)^{1/2}(8x^7 + 6)$
D) $f'(x) = \frac{1}{3}(8x^7 + 6)^{-2/3}$

7) $y = (2x - 1)^3(x + 7)^{-3}$ 7) _____

A) $\frac{dy}{dx} = 45(2x - 1)^3(x + 7)^{-4}$
B) $\frac{dy}{dx} = 45(2x - 1)^2(x + 7)^{-3}$
C) $\frac{dy}{dx} = 45(2x - 1)^2(x + 7)^{-4}$
D) $\frac{dy}{dx} = 45(2x - 1)^3(x + 7)^{-2}$

Find $\frac{d^2y}{dx^2}$.

8) $y = \frac{x}{x+1}$

8) _____

Find the derivative.

9) $y = \frac{8e^x}{2e^x + 1}$

9) _____

A) $\frac{8e^x}{(2e^x + 1)^2}$

B) $\frac{e^x}{(2e^x + 1)^2}$

C) $\frac{8e^x}{(2e^x + 1)^3}$

D) $\frac{8e^x}{(2e^x + 1)^2}$

10) $y = (e^{x^3} - 2)^4$

10) _____

11) $y = e^{x^5} \ln x$

A) $\frac{e^{x^5} + 5e^{x^5} \ln x}{x}$

B) $\frac{e^{x^5} + 5x^5 e^{x^5} \ln x}{x}$

C) $\frac{5x^5 e^{x^5} + 1}{x}$

D) $\frac{e^{x^5} + 5x^4 e^{x^5} \ln x}{x}$

11) _____

$$12) f(x) = \ln(e^{6x} - 5)$$

$$12) \underline{\hspace{2cm}}$$

$$13) f(x) = (\ln x)^7$$

$$13) \underline{\hspace{2cm}}$$

$$14) f(x) = \frac{x+3}{\sqrt[3]{x}}, \text{ find } f'(x)$$

$$14) \underline{\hspace{2cm}}$$

$$A) x^{3/2} + 3\sqrt{x}$$

$$B) \frac{1}{\sqrt[3]{x}} + \frac{3}{x^{3/2}}$$

$$C) \frac{1}{2\sqrt[3]{x}} - \frac{3}{2x^{3/2}}$$

$$D) \frac{1}{2\sqrt[3]{x}} - \frac{3}{2x}$$

Give an appropriate answer.

$$15) \text{ If } g'(4) = -4 \text{ and } h'(4) = -6, \text{ find } f'(4) \text{ for } f(x) = -2g(x) - 2h(x) + 2.$$

$$15) \underline{\hspace{2cm}}$$

Answer Key

Testname: DERIVATIVES SPRING 2016

1) C

2) 2

3) $y = -27x + 54$

4) $-\frac{25}{3}, 7$

5) B

6) B

7) C

8) $-2(x + 1)^{-3}$

9) D

10) $12x^2 e^{x^3} (e^{x^3} - 2)^3$

11) B

12) $\frac{6e^{6x}}{e^{6x} - 5}$

13) $\frac{7(\ln x)^6}{x}$

14) C

15) 20